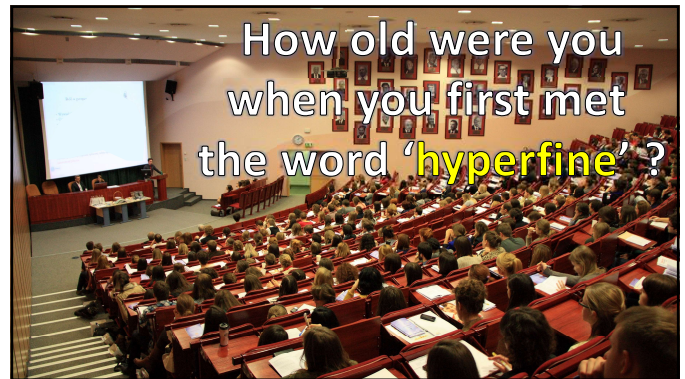




1



2



3

Second

The **second** (symbol: **s**) is the unit of time in the International System of Units (SI), historically defined as $\frac{1}{86400}$ of a day – this factor derived from the division of the day first into 24 hours, then to 60 minutes and finally to 60 seconds each ($24 \times 60 \times 60 = 86400$). "Minute" comes from the Latin *pars minuta prima*, meaning "first small part", and "second" comes from the *pars minuta secunda*, "second small part".

The current and formal definition in the International System of Units (SI) is more precise:

The second [...] is defined by taking the fixed numerical value of the caesium frequency, $\Delta\nu_{\text{Cs}}$, the unperturbed ground-state hyperfine transition frequency of the caesium 133 atom, to be 9 192 631 770 when expressed in the unit Hz, which is equal to s^{-1} .^[1]

This current definition was adopted in 1967 when it became feasible to define the second based on fundamental properties of nature with caesium clocks.^[2] Because the speed of Earth's rotation varies and is slowing ever so slightly, a leap second is added at irregular intervals to civil time^[nb 1] to keep clocks in sync with Earth's rotation.

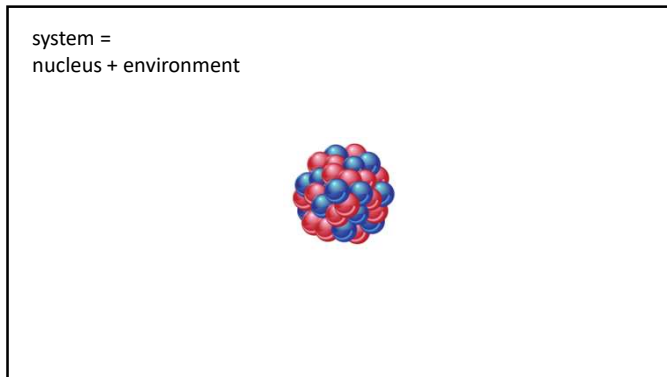
4



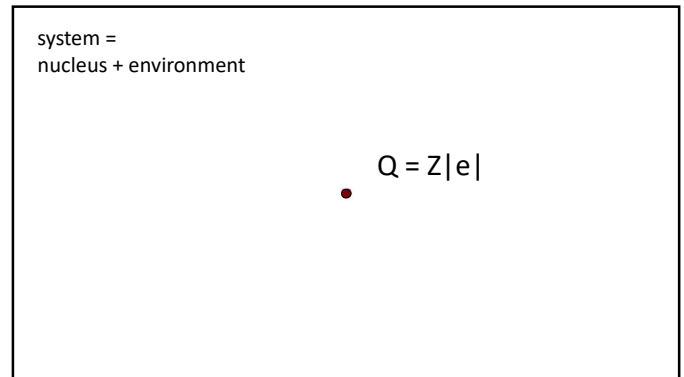
5

define
"system"

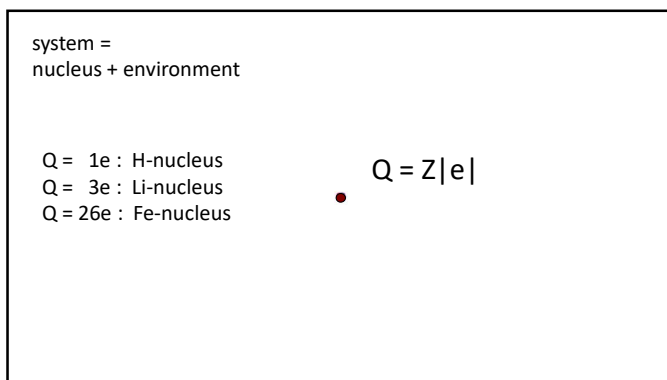
6



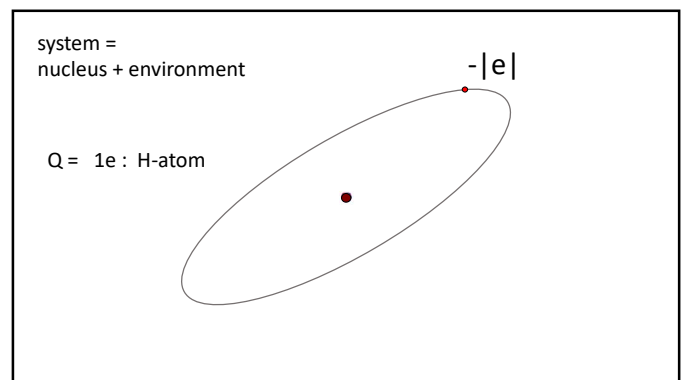
7



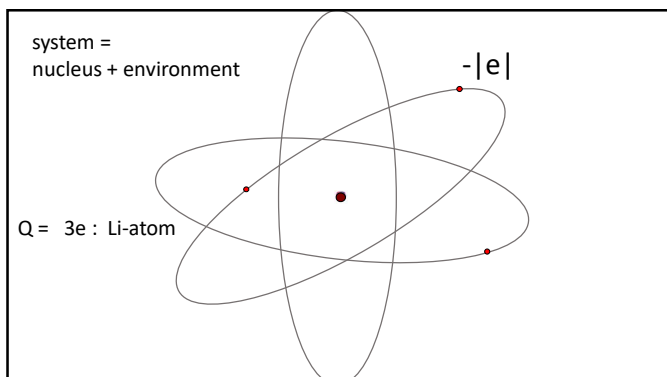
8



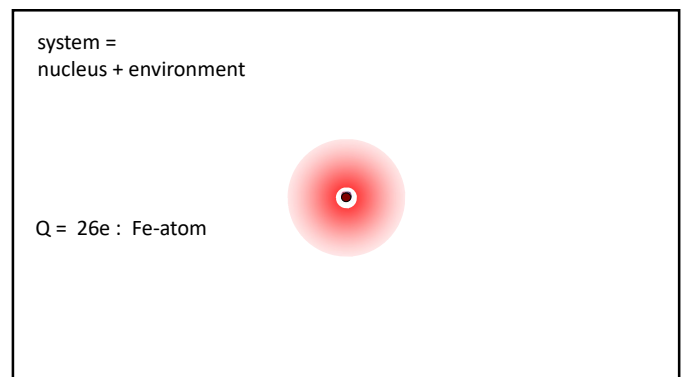
9



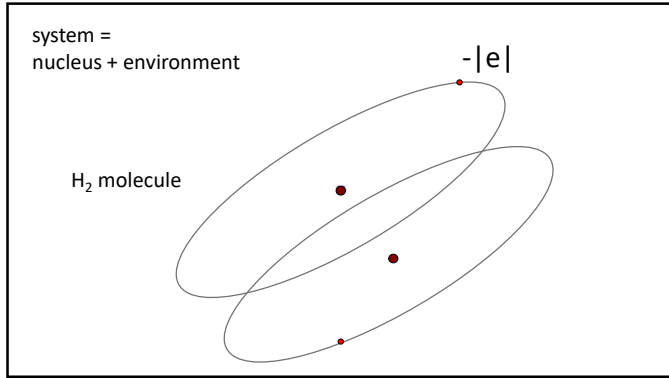
10



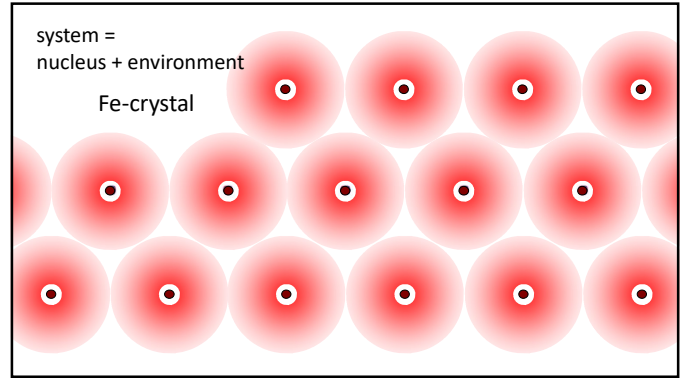
11



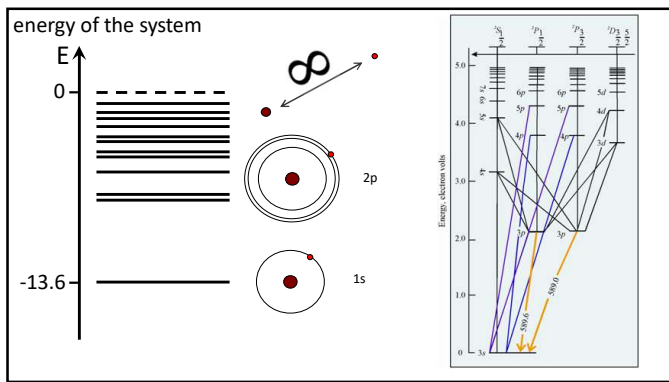
12



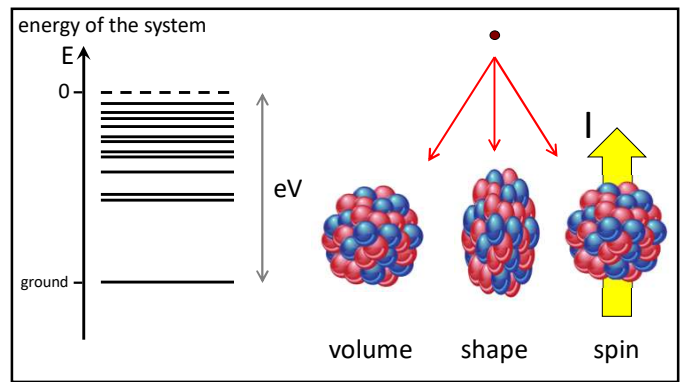
13



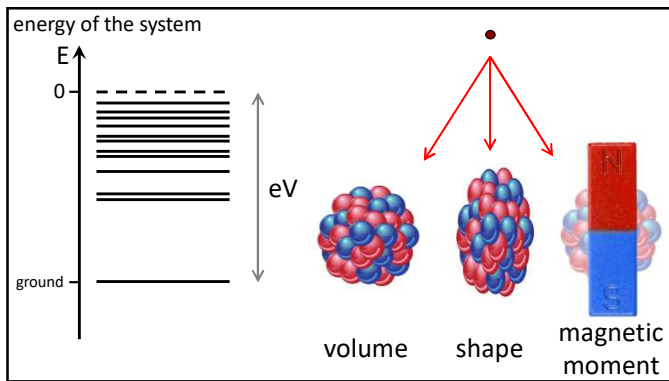
14



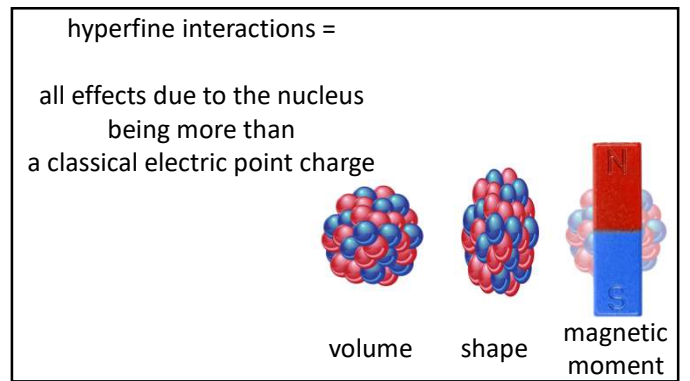
15



16



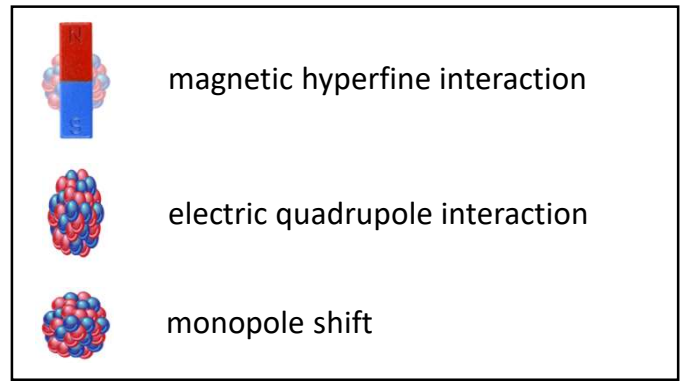
17



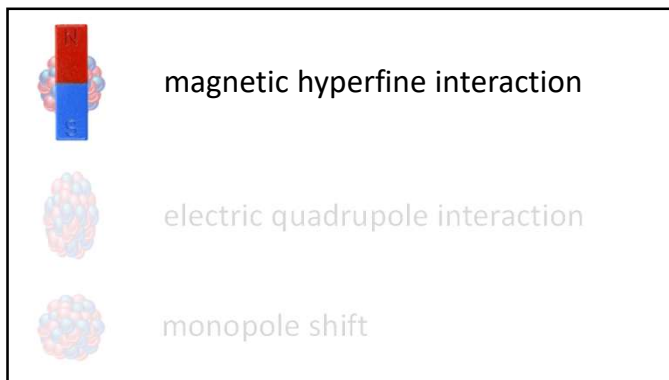
18



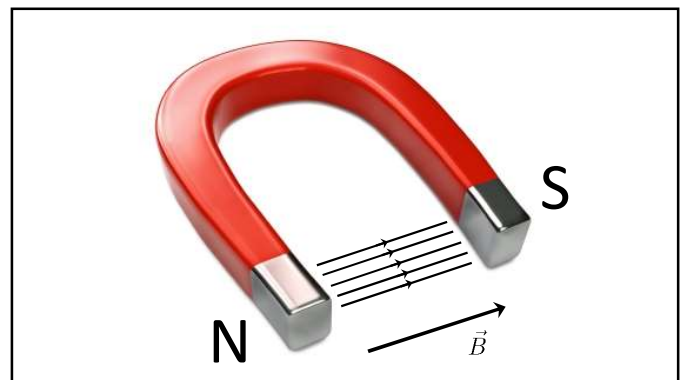
19



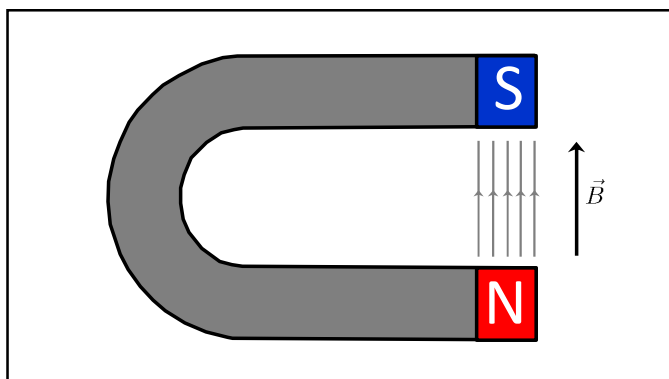
20



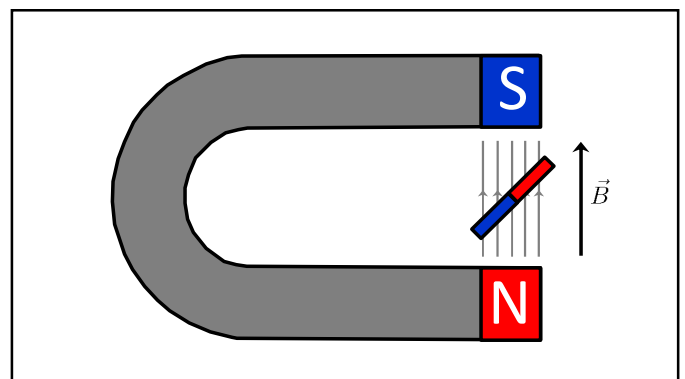
21



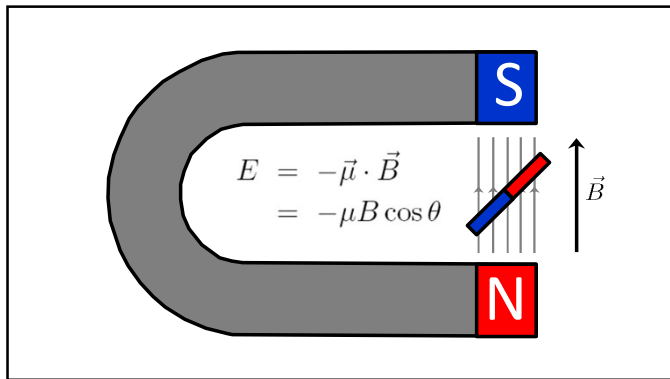
22



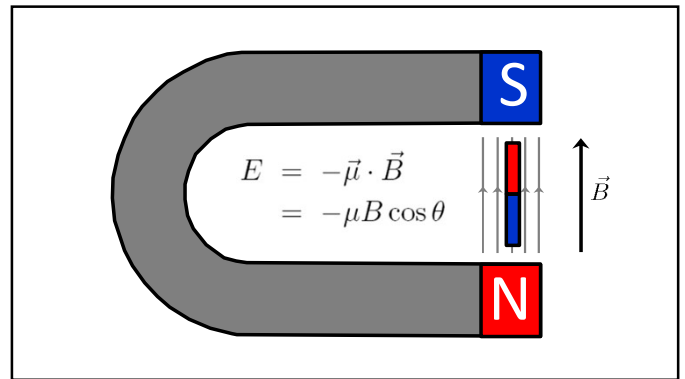
23



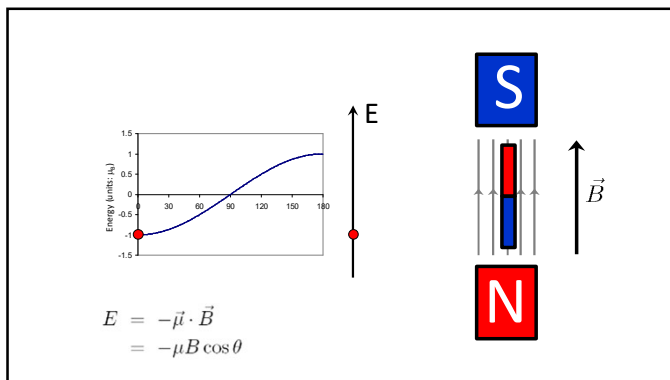
24



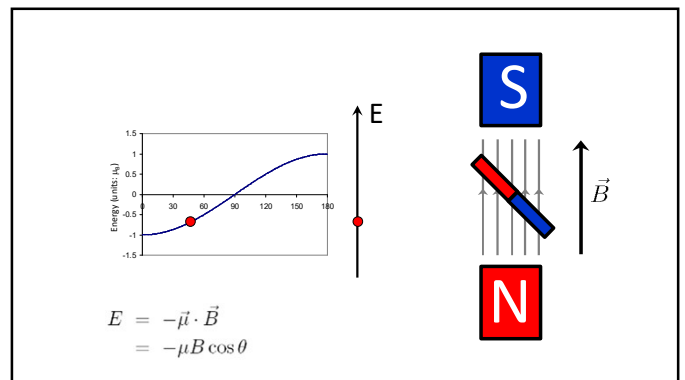
25



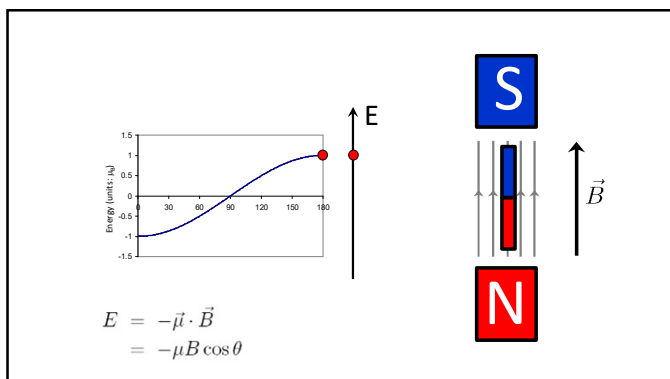
26



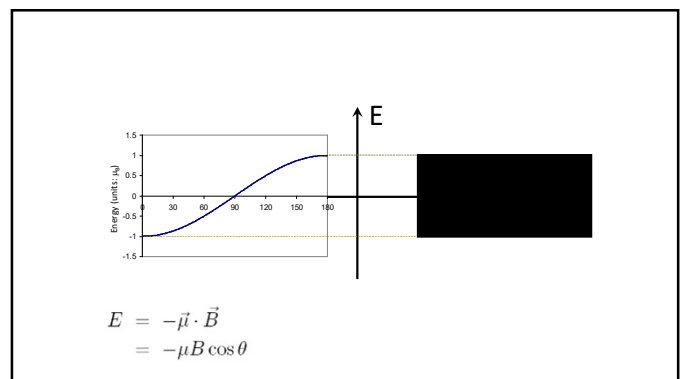
27



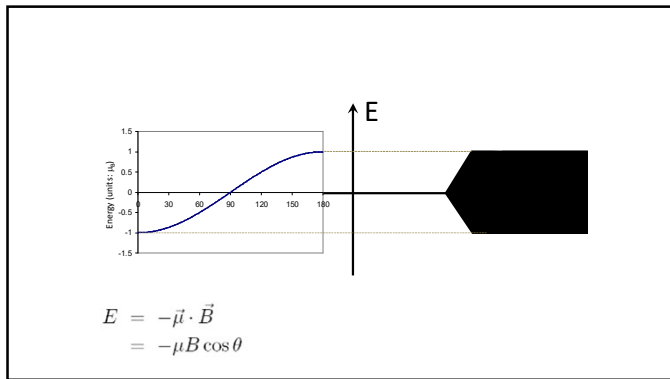
28



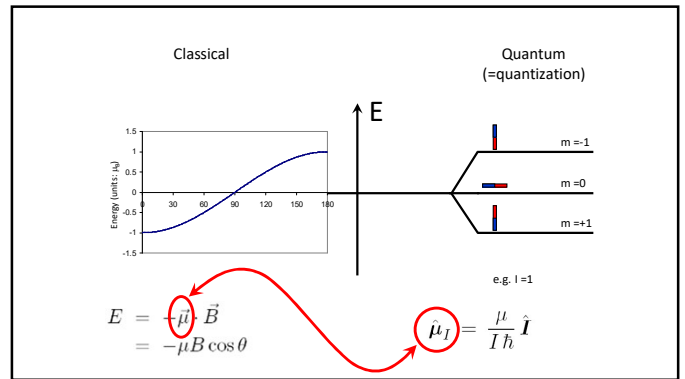
29



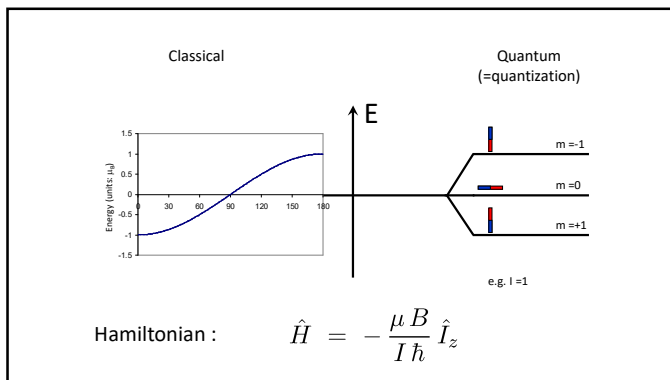
30



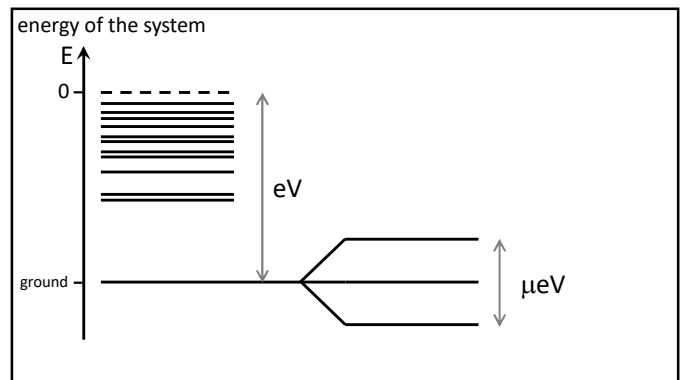
31



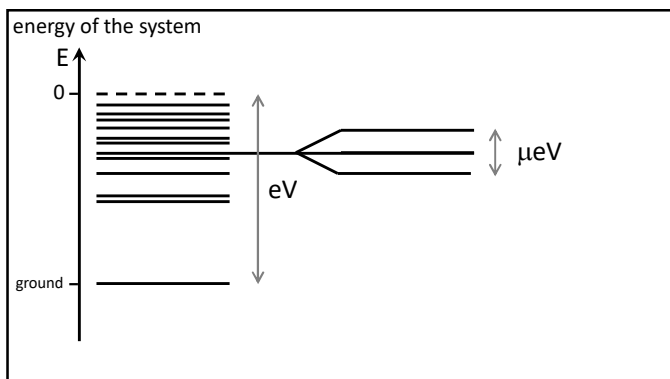
32



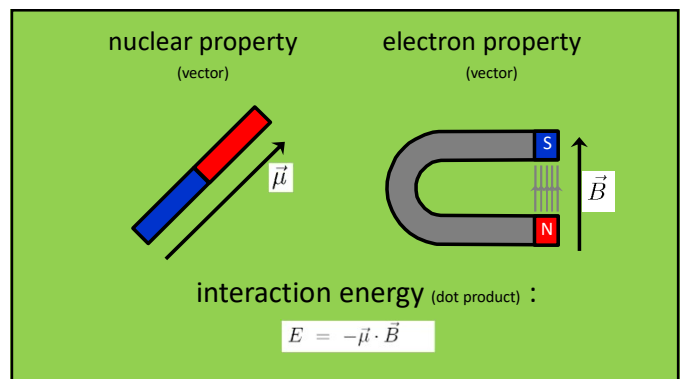
33



34



35



36

Source of magnetic fields at the nuclear site in an atom/solid

$$B_{\text{tot}} = B_{\text{dip}} + B_{\text{orb}} + B_{\text{fermi}} + B_{\text{lat}}$$

- > B_{dip} = electron as bar magnet
- > B_{orb} = electron as current loop
- > B_{fermi} = electron in nucleus
- > B_{lat} = neighbours as bar magnets

$$-\frac{2\mu_B\mu_0}{3} (|\psi_{e, \uparrow}(\mathbf{0})|^2 - |\psi_{e, \downarrow}(\mathbf{0})|^2)$$

37

How to do it in WIEN2k ?

Magnetic hyperfine field

In regular scf file:
:HFxxxx (Fermi contact contribution)

After post-processing with LAPWDM :

- orbital hyperfine field ("3 3" in case.indmc)
- dipolar hyperfine field ("3 5" in case.indmc)

in case.scfdmup

```
----- top of file: case.indmc -----
-3-      Bndv cutoff energy
1       number of atoms for which density matrix is calculated
1 1 2   index of 1st atom, number of l's, ll
0 0     r-index, (l,r)-index
----- bottom of file -----
```

After post-processing with DIPAN :
• lattice contribution

more info:
UG 7.8 (lapwdm)
UG 8.3 (dipan)

38

How to do it in WIEN2k ?

Magnetic hyperfine field

In regular scf file:
:HFxxxx (Fermi contact)

After post-processing with LAPWDM :

- orbital hyperfine field ("3 3" in case.indmc)
- dipolar hyperfine field ("3 5" in case.indmc)

in case.scfdmup

```
----- top of file: case.indmc -----
-3-      Bndv cutoff energy
1       number of atoms for which density matrix is calculated
1 1 2   index of 1st atom, number of l's, ll
0 0     r-index, (l,r)-index
----- bottom of file -----
```

After post-processing with DIPAN :
• lattice contribution

more info:
UG 7.8 (lapwdm)
UG 8.3 (dipan)

39

magnetic hyperfine interaction

electric quadrupole interaction

monopole shift

40

$Q = \text{charge on plate}$ | $\text{Plate area } A$

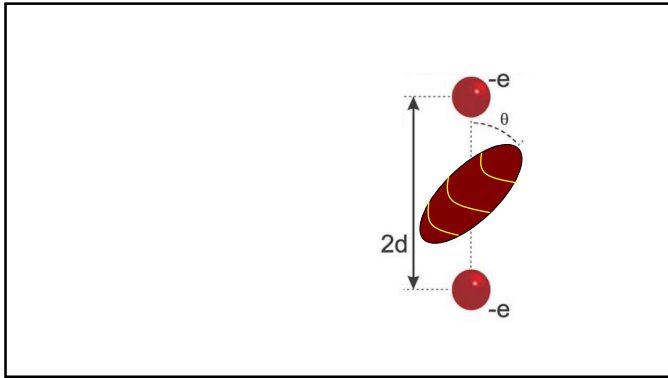
$E = \frac{\sigma}{\epsilon} = \frac{V}{d}$

41

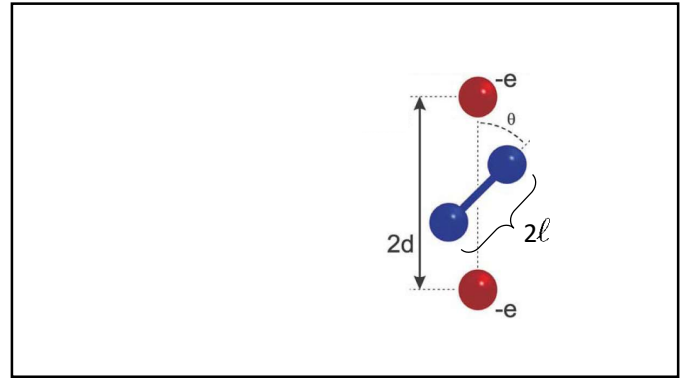
- Force on a point charge:
$$\vec{F} = Q\vec{E}$$
- Force on a general charge:
$$\vec{F} = \int \vec{E} dQ$$

$$= Q\vec{E}$$

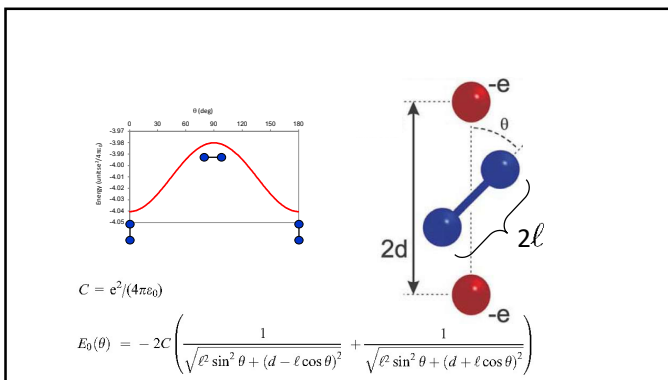
42



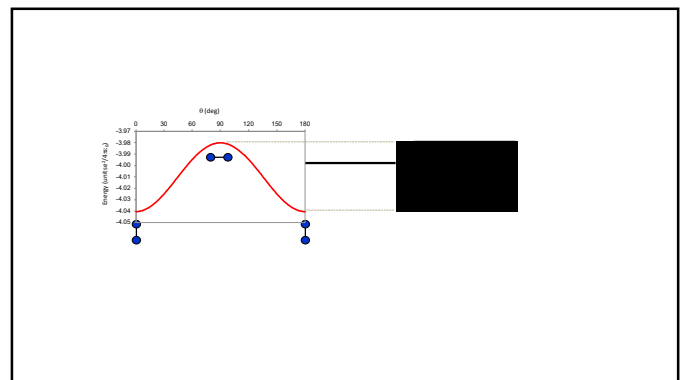
43



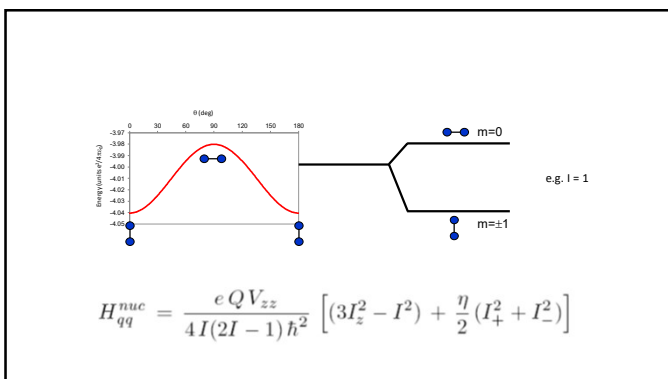
44



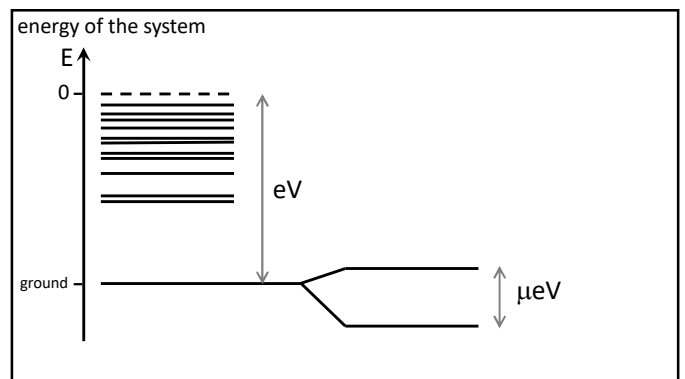
45



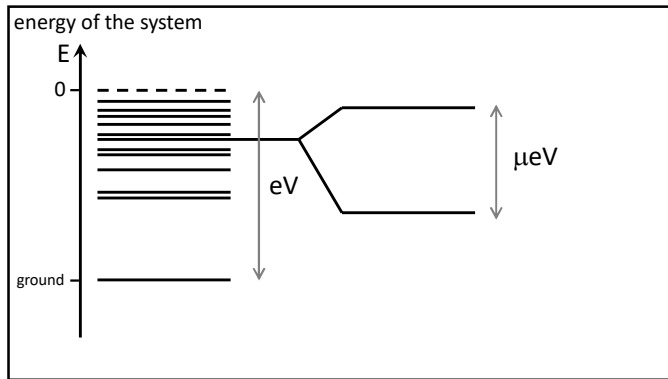
46



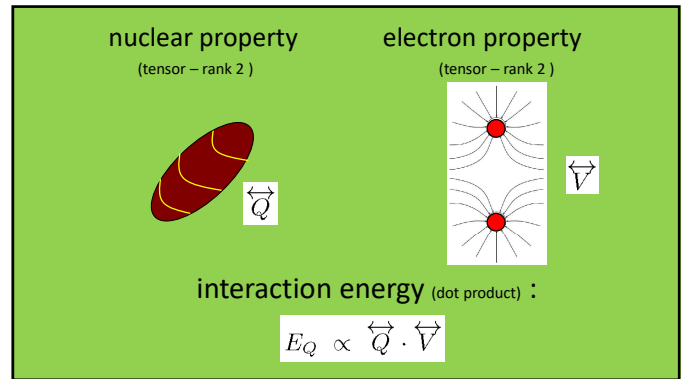
47



48



49



50

How to do it in WIEN2k ?

Electric-field gradient

In regular scf file:

```

: EFGxxx
: ETAxxx
Main directions of the EFG
    
```

} 5 degrees of freedom

Full analysis printed in case.output2 if EFG keyword in case.in2 is put (UG 7.6) (split into many different contributions)

more info:

- Blaha, Schwarz, Dederichs, PRB 37 (1988) 2792
- EFG document in wien2k FAQ (Katrin Koch, SC)

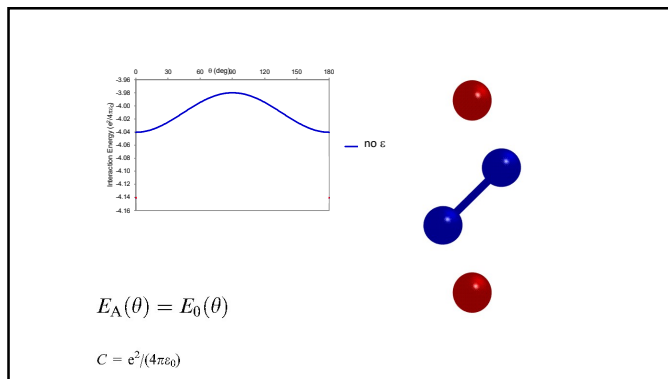
51

magnetic hyperfine interaction

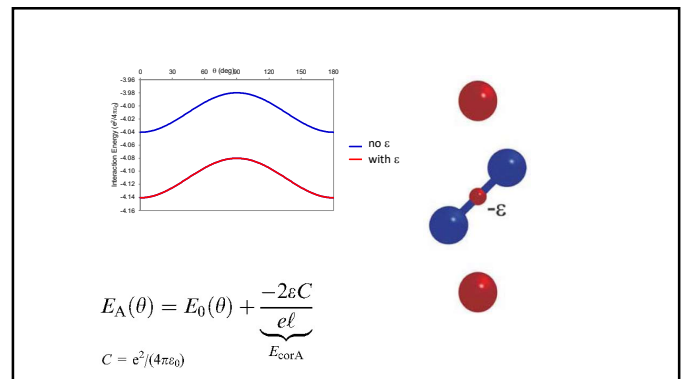
electric quadrupole interaction

monopole shift

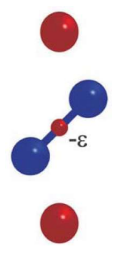
52



53



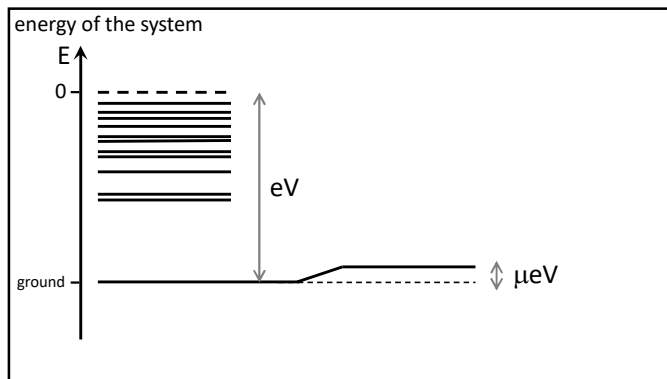
54

$$-\frac{2C}{e} \frac{\epsilon}{\ell} = -\frac{2C}{e} \left(\frac{\epsilon}{\ell^3} \right) \ell^2$$


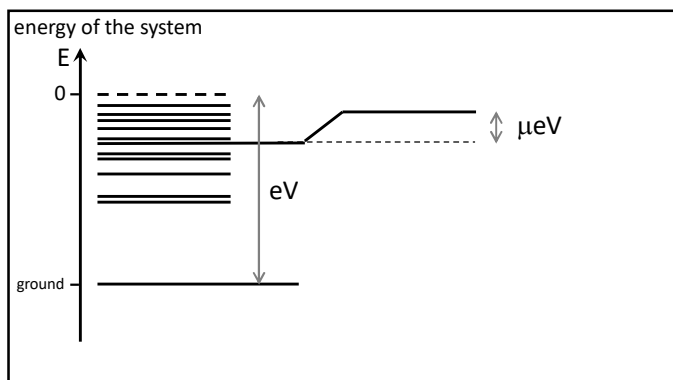
$$E_A(\theta) = E_0(\theta) + \underbrace{\frac{-2\epsilon C}{e\ell}}_{E_{\text{corA}}}$$

$C = e^2/(4\pi\epsilon_0)$

55


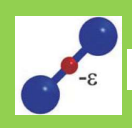


56



57

nuclear property (scalar) electron property (scalar)

interaction energy (dot product):

$$E \propto \langle R^2 \rangle \cdot \rho(0)$$

58







How to do it in WIEN2k ?

Isomer shift calculations

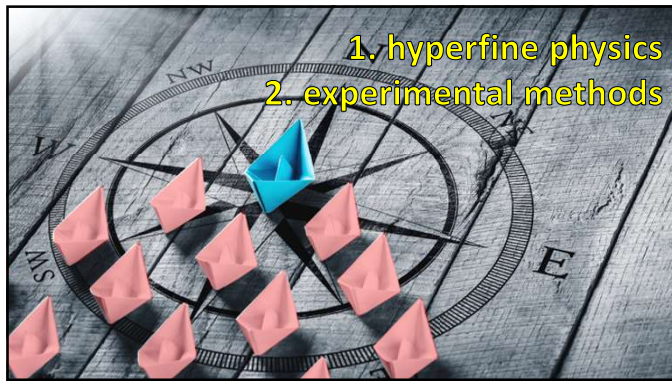
In regular scf file:

:RTOxxx = electron density near the nucleus of atom xxx (i.e. at the first radial mesh point, typically 0.0005 au)

59

rank	nuclear property	•	electron property
		(dot product)	
0	volume 		
1	magnetic moment 		
2	shape 		

60



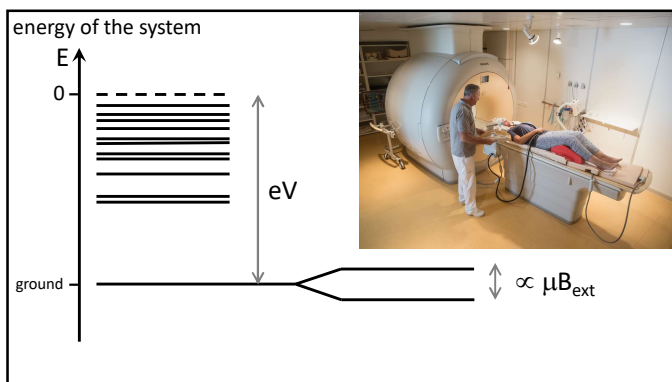
61

experimental hyperfine methods =

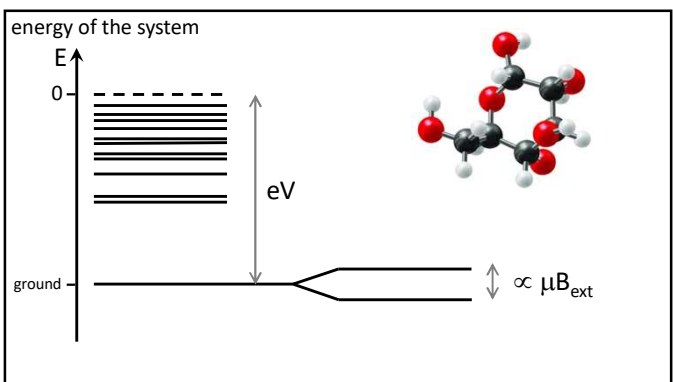
all methods of which the experimental signal is affected by a nucleus that is more than a classical electric point charge

All methods that are based on transitions between levels that are shifted or split by hyperfine interactions

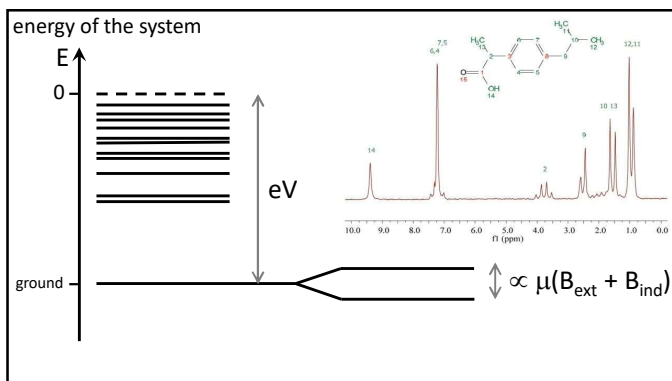
62



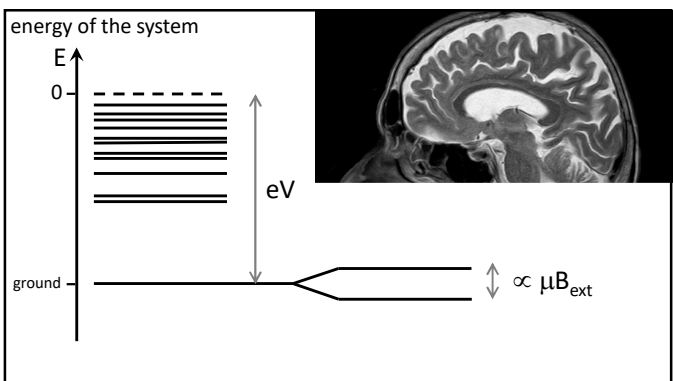
63



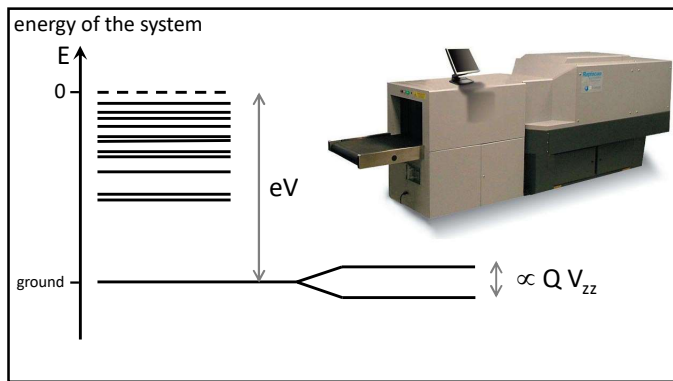
64



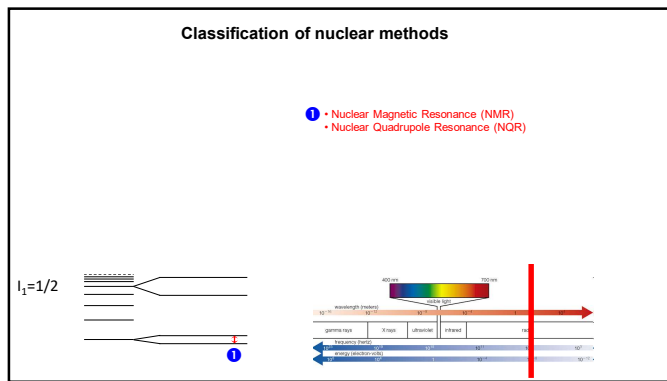
65



66



67



68

Second

The second (symbol: s) is the unit of time in the International System of Units (SI), historically defined as $\frac{1}{86400}$ of a day – this factor derived from the division of the day first into 24 hours, then to 60 minutes and finally to 60 seconds each ($24 \times 60 \times 60 = 86400$). "Minute" comes from the Latin *pars minuta prima*, meaning "first small part", and "second" comes from the *pars minuta secunda*, "second small part".

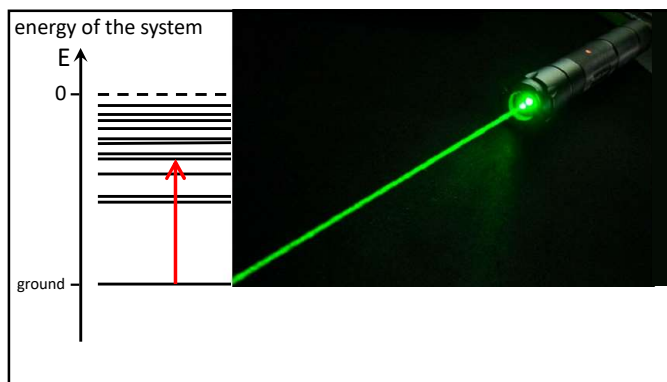
The current and formal definition in the International System of Units (SI) is more precise:

The second [...] is defined by taking the fixed numerical value of the caesium frequency, $\Delta\nu_{Cs}$, the unperturbed ground-state hyperfine transition frequency of the caesium-133 atom, to be 9 192 631 770 when expressed in the unit Hz, which is equal to s^{-1} .^[1]

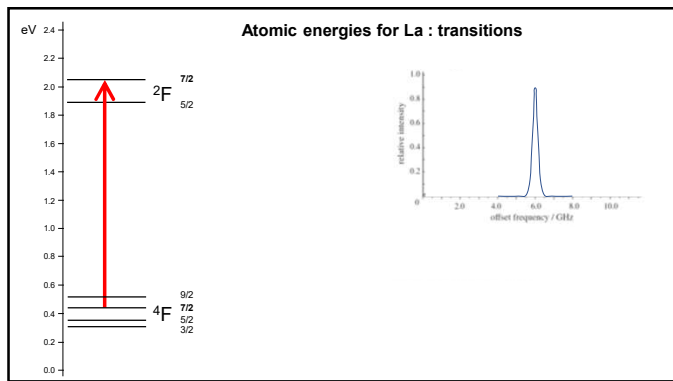
This current definition was adopted in 1967 when it became feasible to define the second based on fundamental properties of nature with caesium clocks.^[2] Because the speed of Earth's rotation varies and is slowing ever so slightly, a leap second is added at irregular intervals to civil time^[1b] to keep clocks in sync with Earth's rotation.

atomic clocks with the Cs standard use this principle

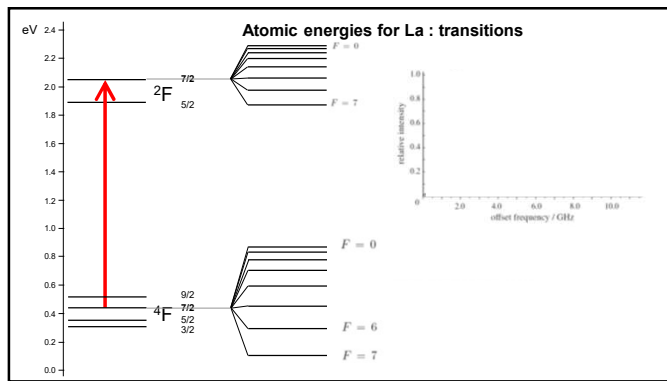
69



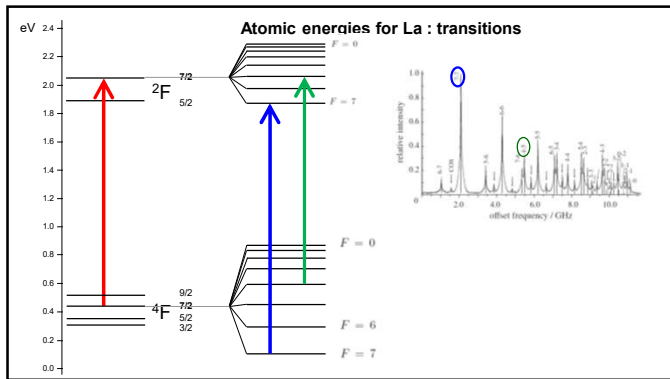
70



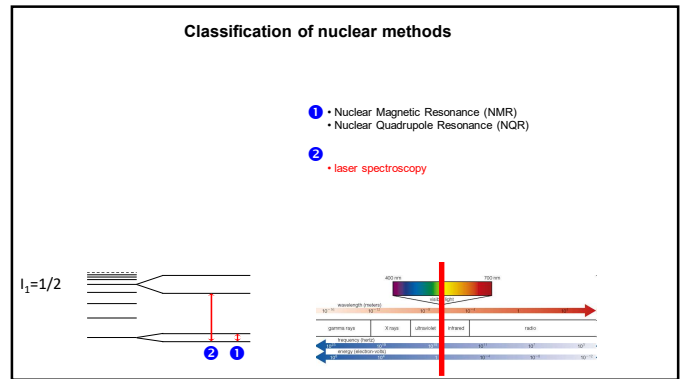
71



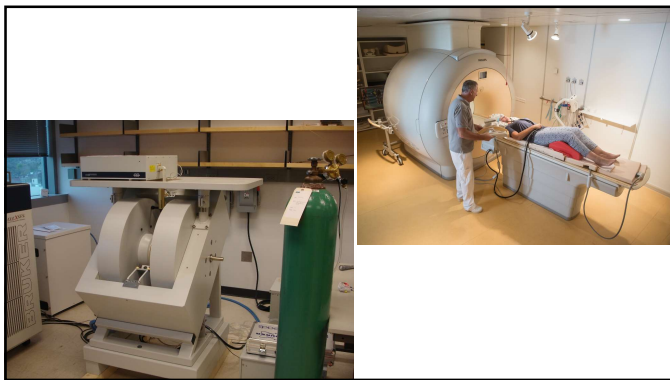
72



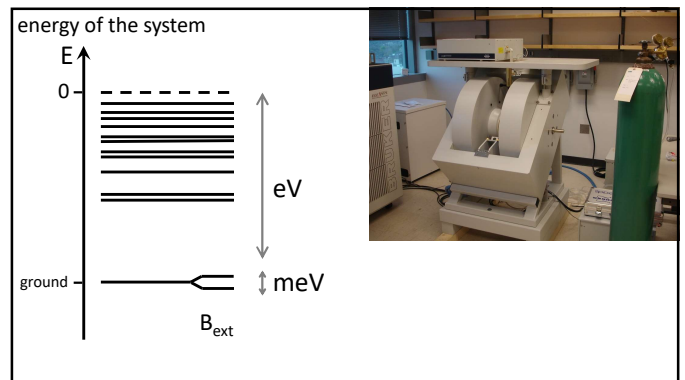
73



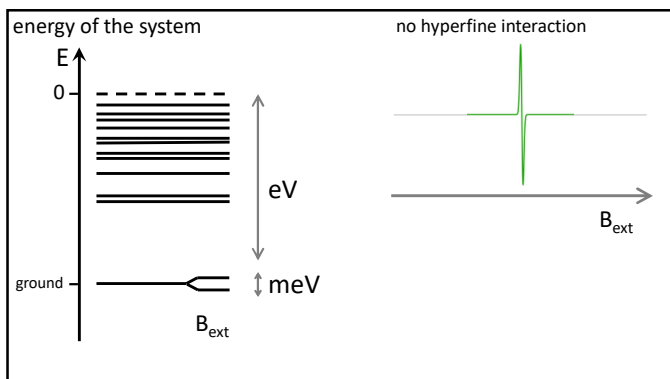
74



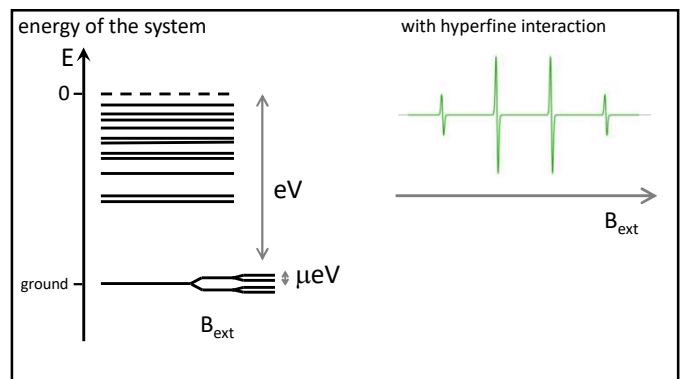
75



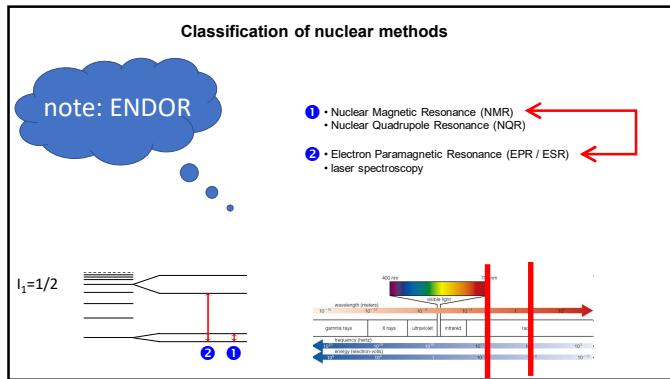
76



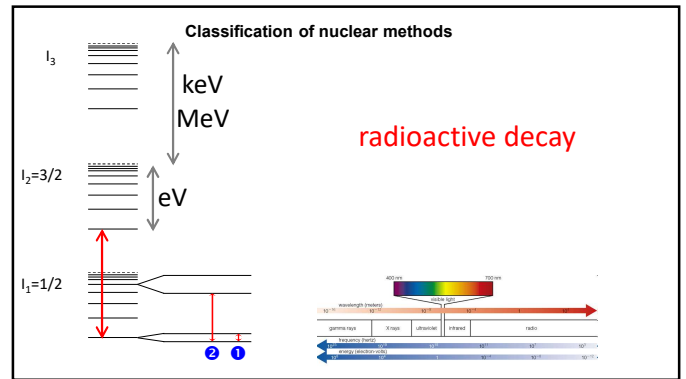
77



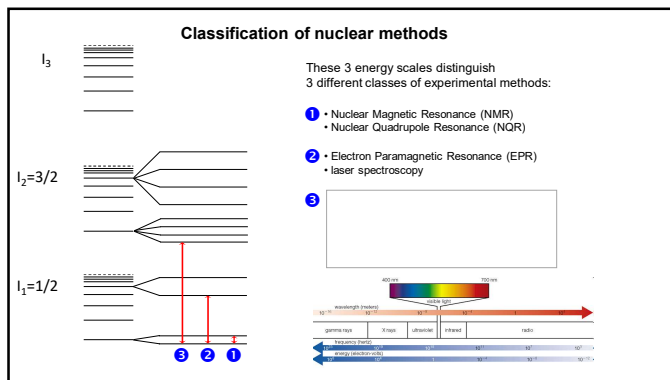
78



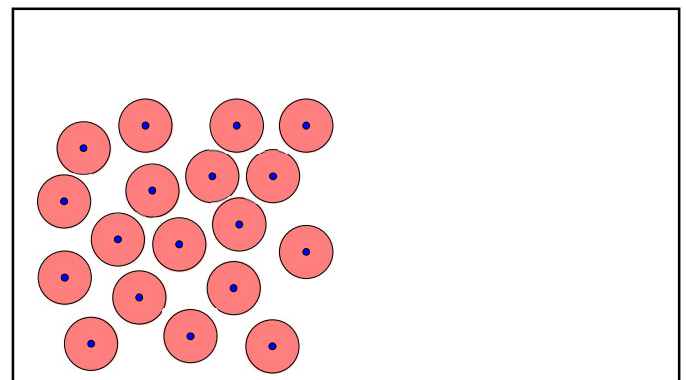
79



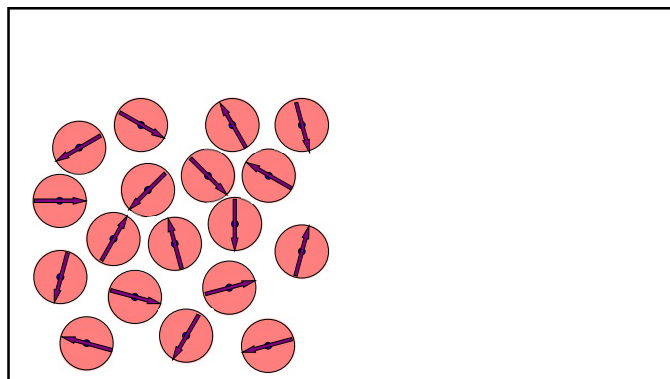
80



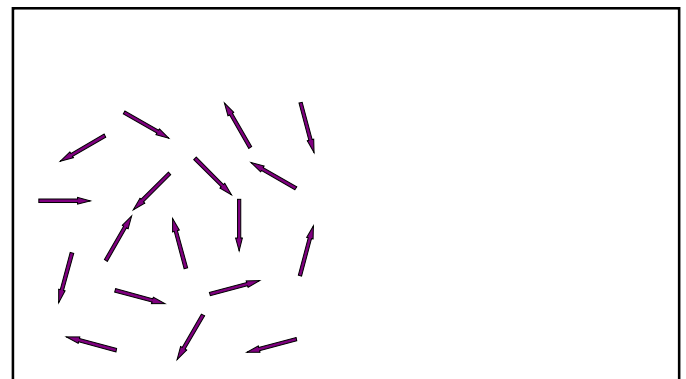
81



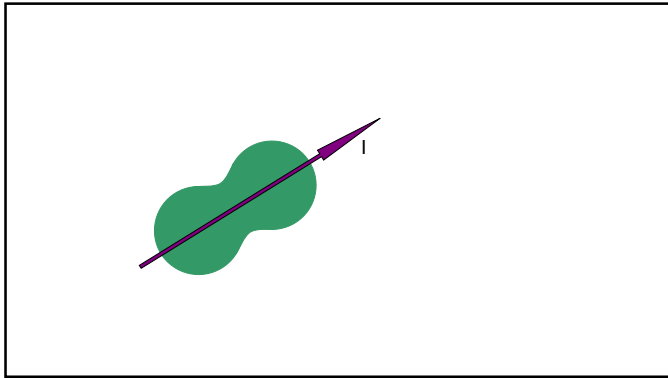
82



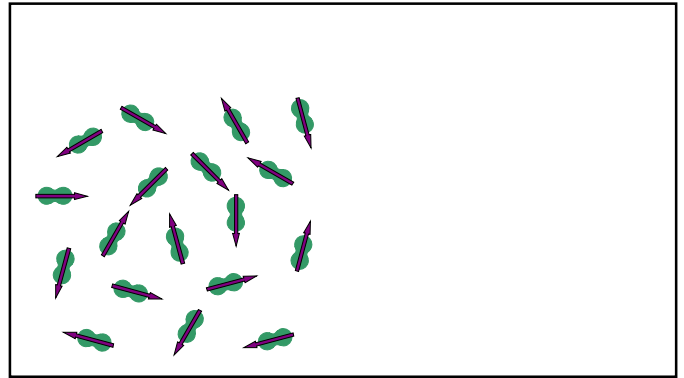
83



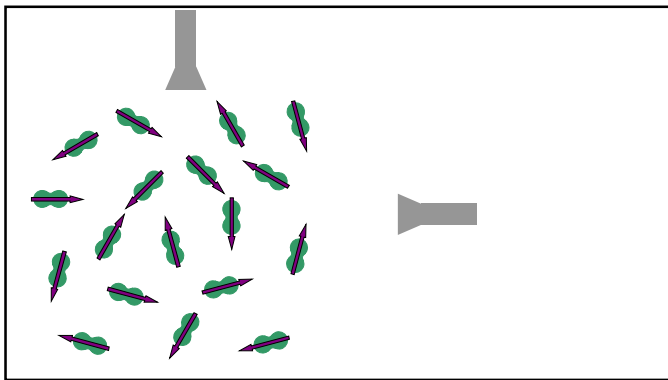
84



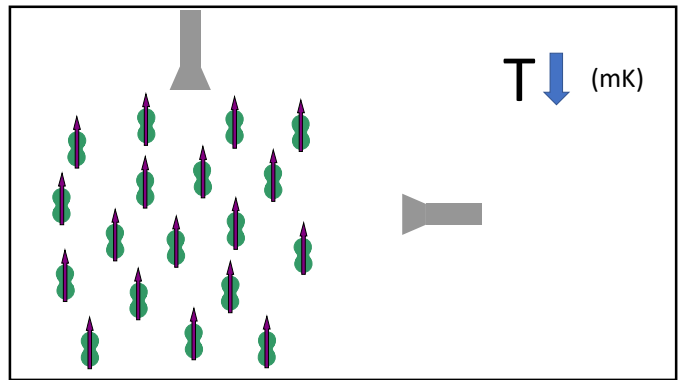
85



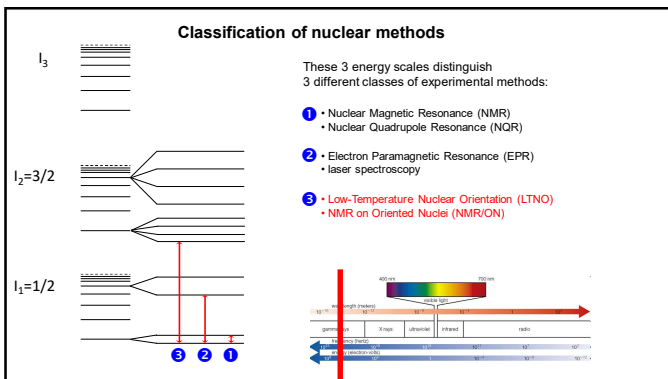
86



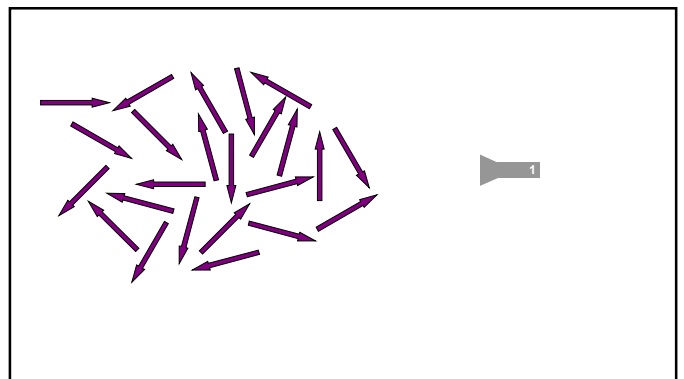
87



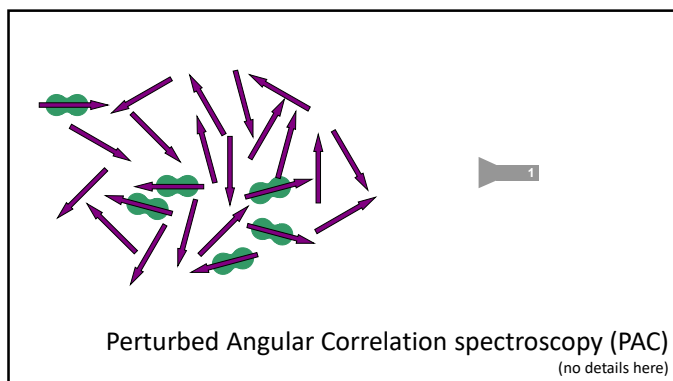
88



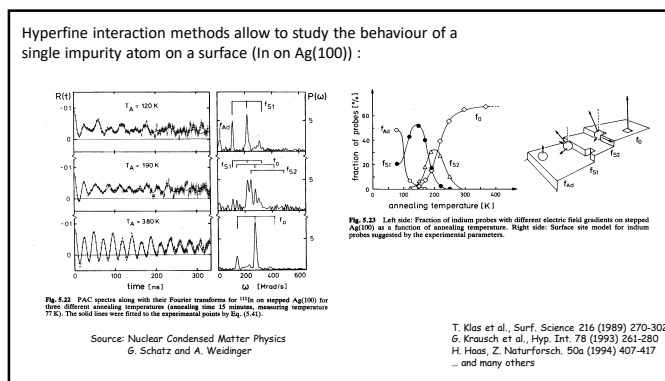
89



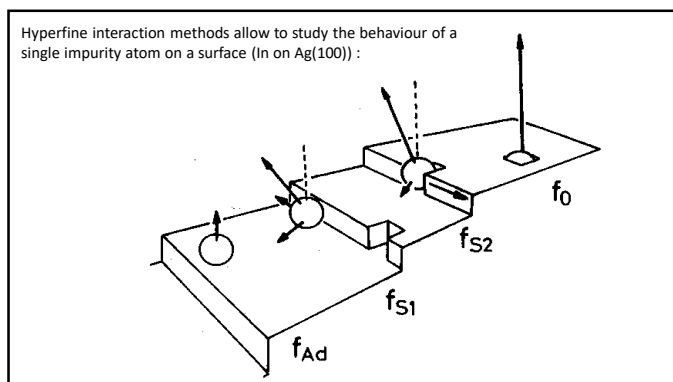
90



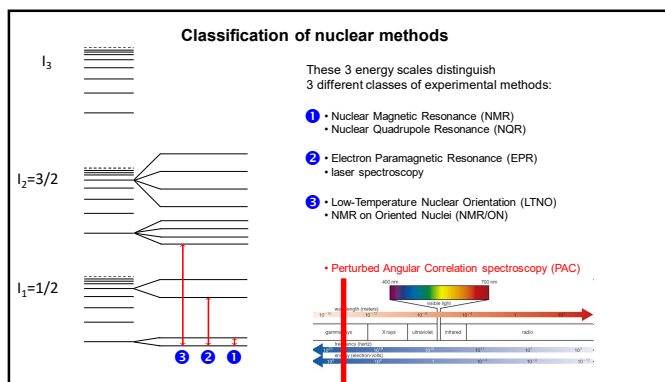
91



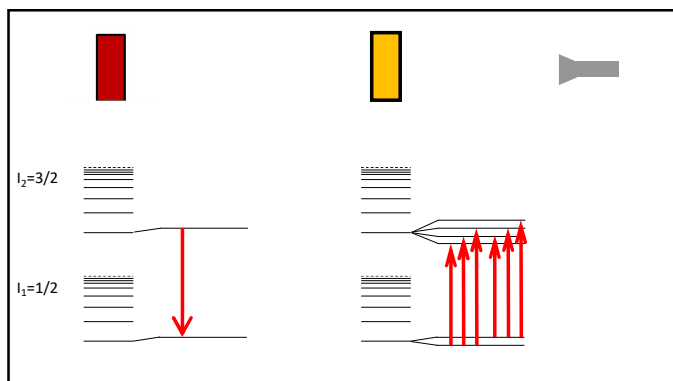
92



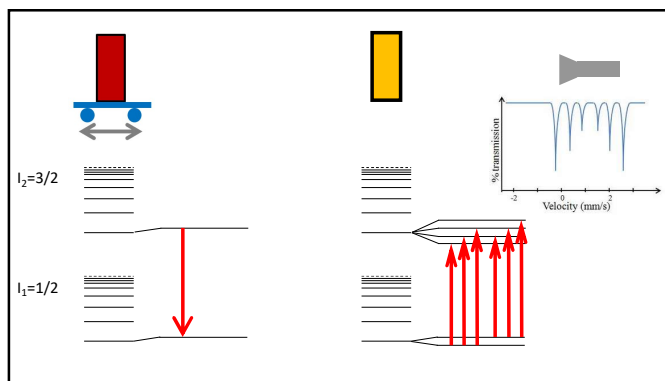
93



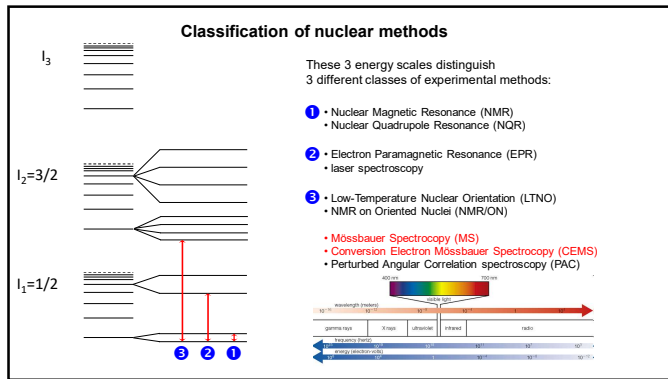
94



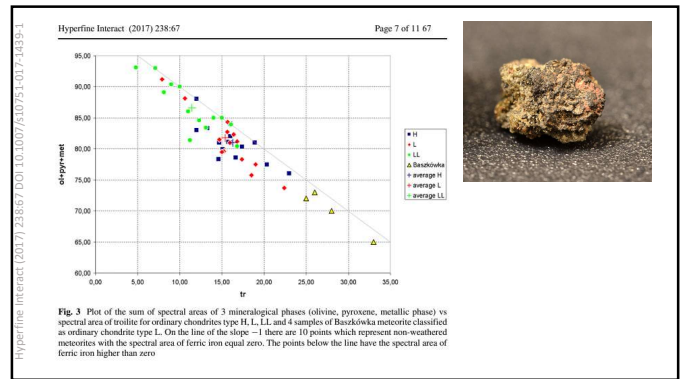
95



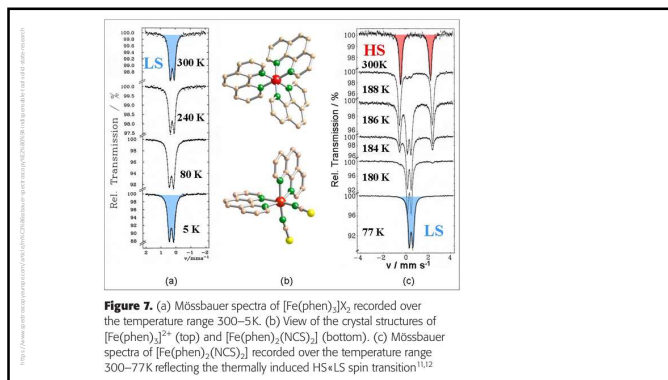
96



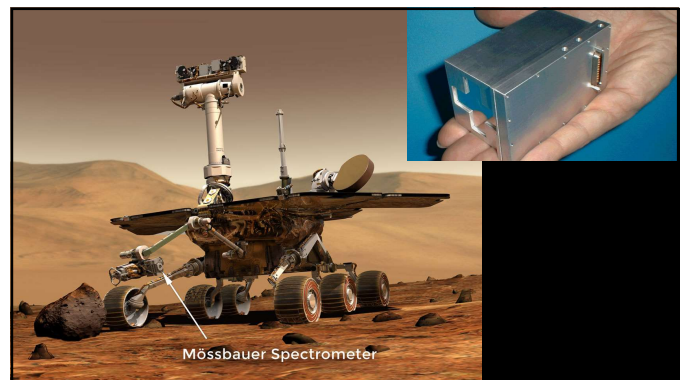
97



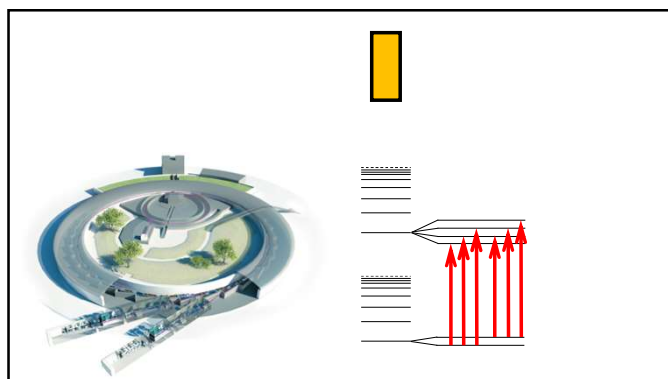
98



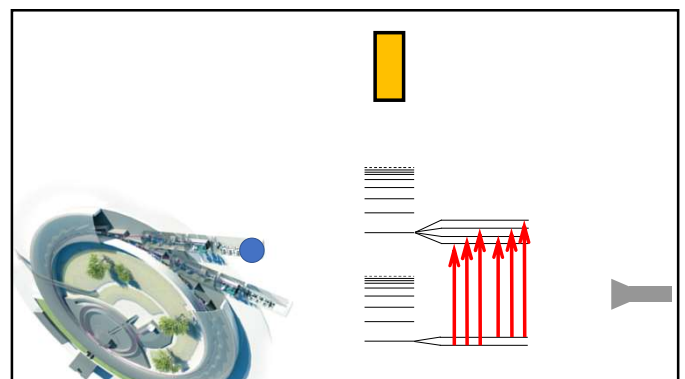
99



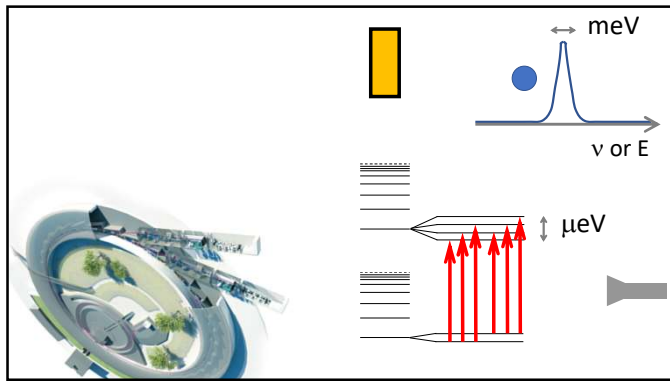
100



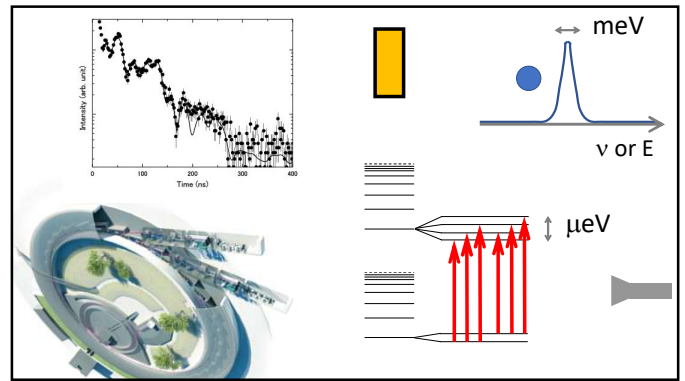
101



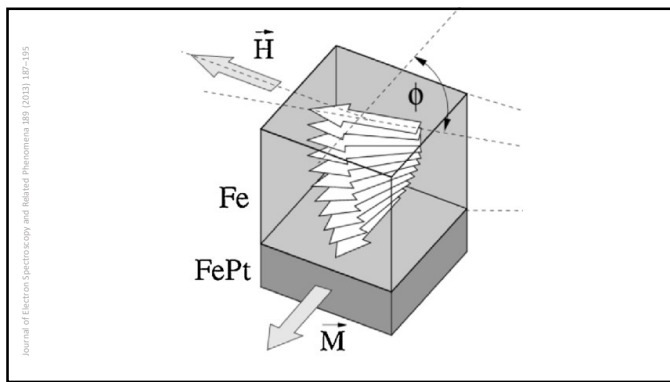
102



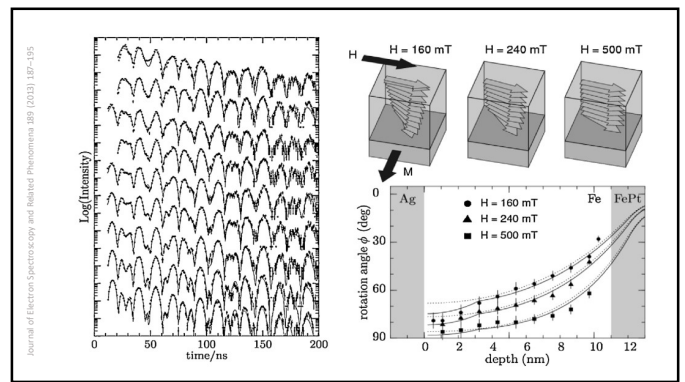
103



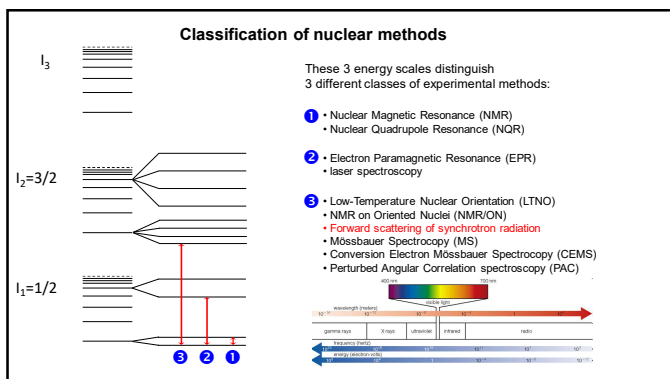
104



105









106



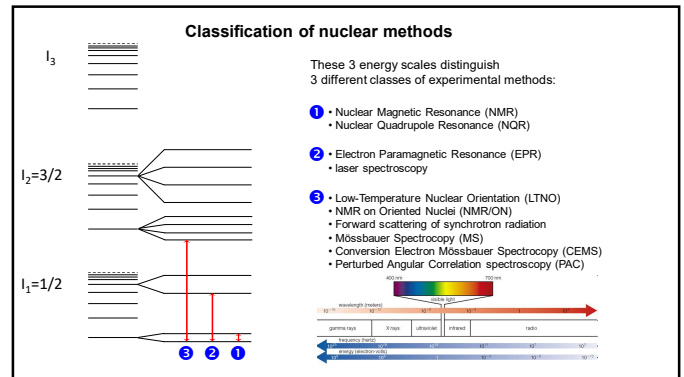
107



108

rank	nuclear property • electron property (dot product)
0	<div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>volume</p>  </div> <div style="text-align: center;">  </div> </div>
1	<div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>magnetic moment</p>  </div> <div style="text-align: center;">  </div> </div>
2	<div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>shape</p>  </div> <div style="text-align: center;">  </div> </div>

109



110



111

want to study more ? www.hyperfinecourse.org



Didactical philosophy behind this course: <https://youtu.be/YsUk4P1f5DM>

112

short version of this talk (with WIEN2k instructions) :

https://youtu.be/TErBA54sk_Y

45-minute version (as today) but without WIEN2k instructions :

https://youtu.be/_cMNUQB3fi

step-by-step demo video for hyperfine fields with WIEN2k :

<https://youtu.be/L4t5ZAJAsoY>

course: www.hyperfinecourse.org

didactical approach : <https://youtu.be/YsUk4P1f5DM>

my Youtube channel : <https://bit.ly/cottenier>
 stefaan.cottenier@ugent.be

113